



INSTITUTE FOR DEFENSE ANALYSES

**Estimating Hedonic Price Indices
for Ground Vehicles
(Presentation)**

David M. Tate
Stanley A. Horowitz

June 2015

Approved for public release;
distribution is unlimited.

IDA Document NS D-5525

H 15-000597



The Institute for Defense Analyses is a non-profit corporation that operates three federally funded research and development centers to provide objective analyses of national security issues, particularly those requiring scientific and technical expertise, and conduct related research on other national challenges.

About This Publication

This work was conducted by the Institute for Defense Analyses (IDA) under contract HQ0034-14-D-0001, Project Number BA-7-3054, "Cost Indices Assessment" for the Director, Cost Assessment and Program Evaluation. The views, opinions, and findings should not be construed as representing the official position of either the Department of Defense or the sponsoring organization.

Copyright Notice

© 2015 Institute for Defense Analyses
4850 Mark Center Drive, Alexandria, Virginia 22311-1882 • (703) 845-2000.

This material may be reproduced by or for the U.S. Government pursuant to the copyright license under the clause at DFARS 252.227-7013 (a)(16) [Jun 2013].

Estimating Hedonic Price Indices for Ground Vehicles

**David Tate and Stan Horowitz
Institute for Defense Analyses,
Cost Analysis and Research Division**

IDA | Estimating Price Indices

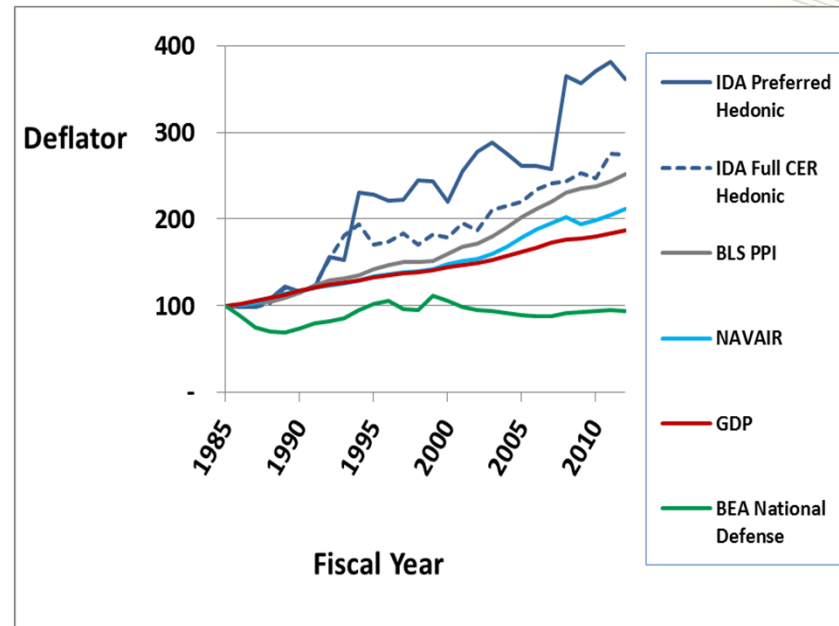
- Price indices are normally estimated by comparing the observed prices of identical goods in successive years
- This is easy when goods don't change much from year to year
 - Milk, gasoline, haircuts, ...
- When the characteristics of products for sale change too quickly, we need to correct for quality changes to estimate real price growth
 - Computers, cell phones, military aircraft...

IDA | Quality-Adjusted Price Indices

- There are two main approaches to quality-adjusted price indices
 - Estimate the amount of price change due to new features for each new product on a case-by-case basis; assign any additional change to real price growth
 - Construct a *hedonic* model of price change that predicts price as a stable function of quality attributes; use annual fixed effects to capture cumulative real price growth

IDA | Previous Work

- Earlier work at IDA looked at military aircraft prices
- Published price indices disagreed wildly
- Indices from BEA estimated near-zero real price growth for decades
- IDA identified a potential systematic bias in those estimates, and estimated much higher price growth for a fixed quality level
- The IDA methodology made extensive use of lot-by-lot aircraft empty weight as a proxy for unobserved quality improvements



IDA | Ground Vehicle Prices

- The goal of this work was to extend the IDA methodology to estimate a hedonic price index (or indices) for military ground vehicles
- Available data had uneven reliability and varying definitions of “price”
 - Selected Acquisition Report – total cost/quantity
 - President’s Budget – vehicle-only cost/quantity
 - MRAP contract data from CAPE-CA
 - Contract announcements from infoBASE
 - Jane’s, FAS, contractor websites, etc.

IDA | Hedonic Specification

- The best hedonic model specification used 8 quality variables
 - 3 continuous
 - 5 binary
 - Lot size
 - Learning by doing
 - Only relevant for 2 out of 40+ vehicle types
 - Log-log specification
- Power density (hp /ton)
 - Top speed
 - Ground pressure (psi)
 - Tracked?
 - Combat?
 - Turret?
 - Armored?
 - Derivative design?

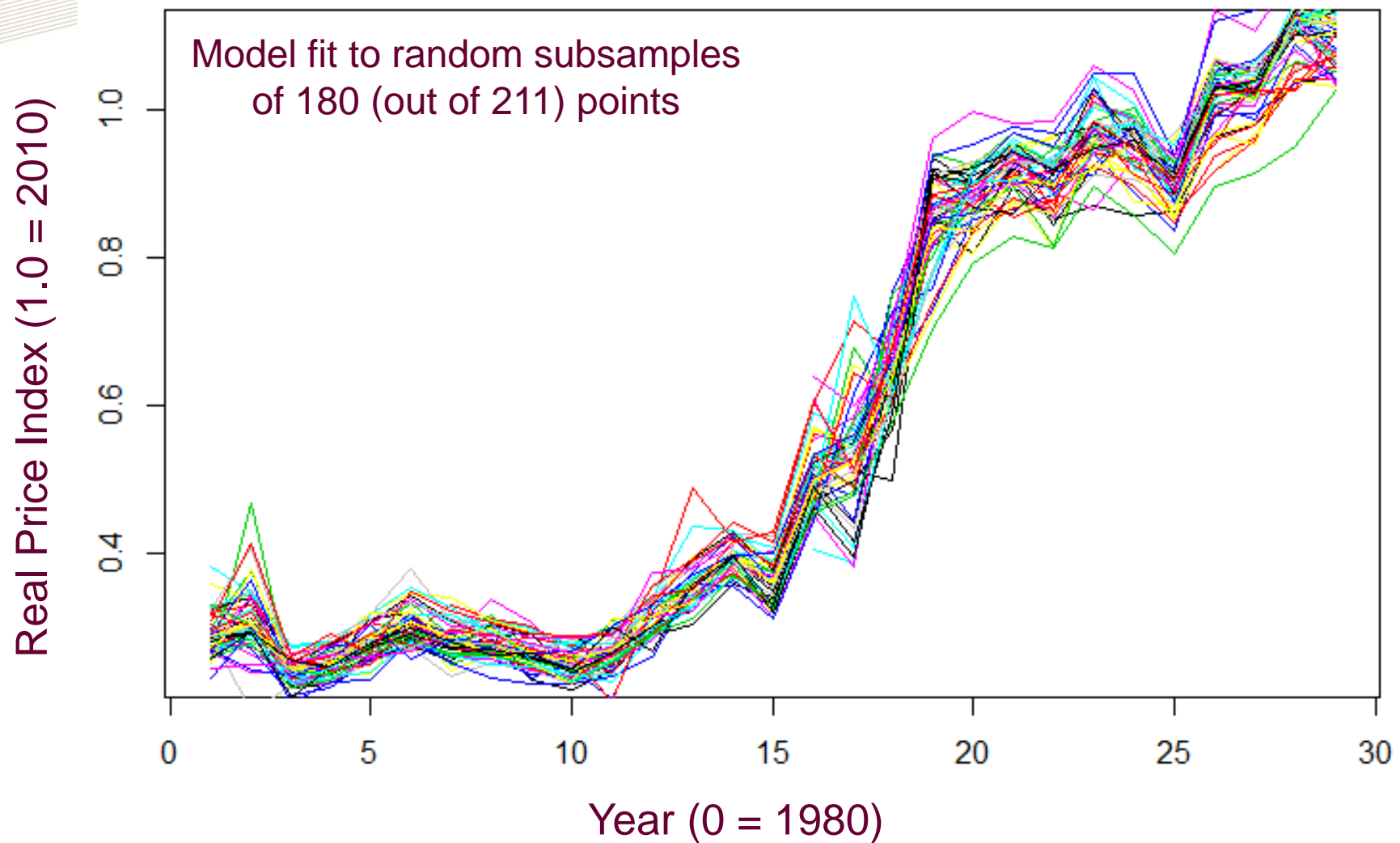
IDA | Predictors Highly Significant...

Parameter	Estimate	Standard Error	
(Intercept)...	9.35	1.35	***
log(Top Speed)...	-2.28	0.26	***
log(Ground Pressure)...	-0.94	0.13	***
log(Gross Vehicle Weight)...	0.93	0.06	***
Armored?...	0.93	0.10	***
Tracked?...	-1.66	0.26	***
Combat?...	0.78	0.06	***
Turret?...	0.49	0.09	***
Derivative?...	-0.28	0.07	***
log(Lot Size)...	-0.07	0.01	***
M9_ACE learning slope...	-0.17	0.04	***
M992_FAASV learning slope...	-0.10	0.03	***

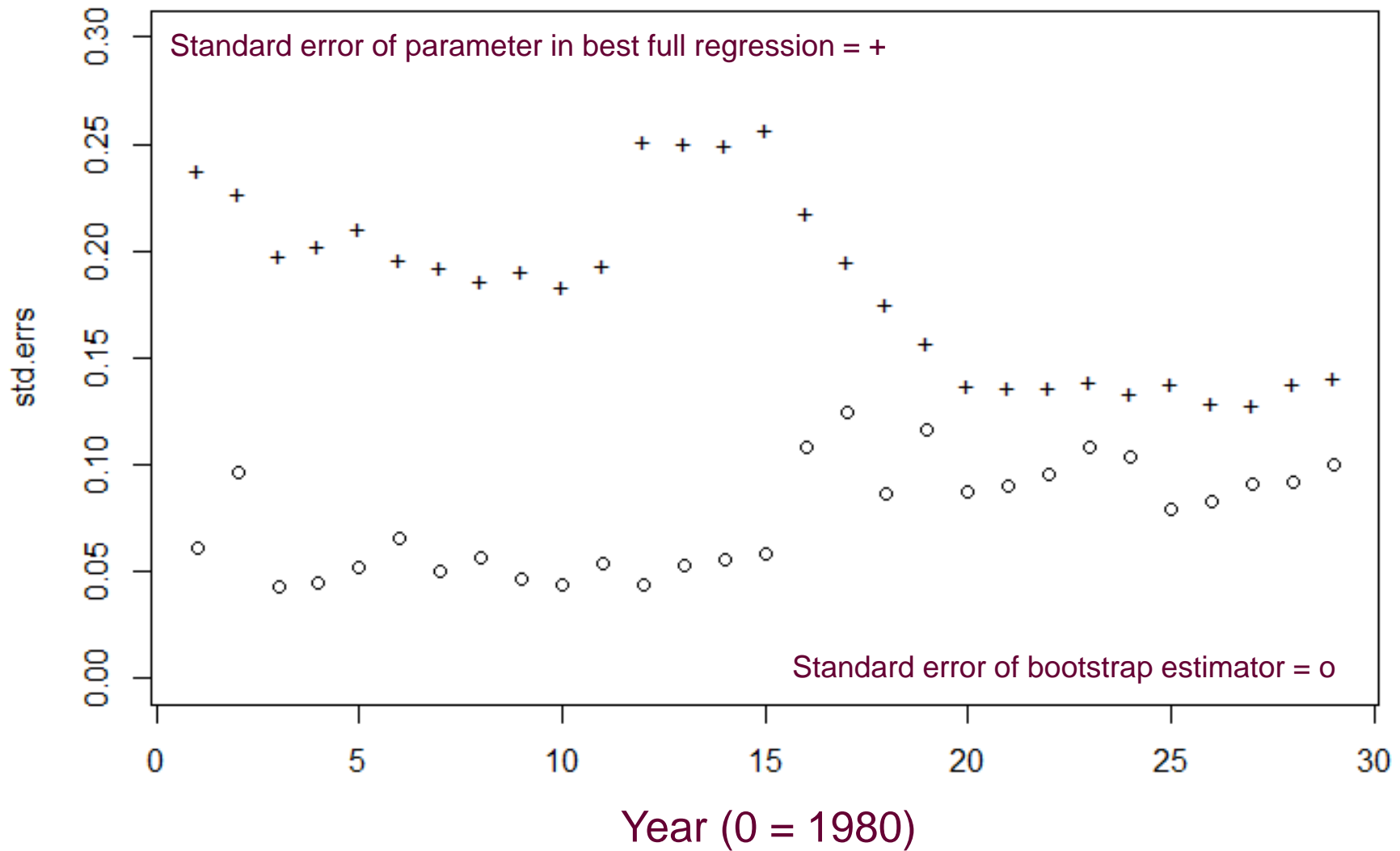
Residual SE...	0.198
Degrees of freedom...	139
Adjusted R ² ...	0.975

All p-values < 10⁻⁵

IDA | Annual Fixed Effect Estimates Were Not Robust



IDA | Bootstrapping Reduced the Fixed Effect SE



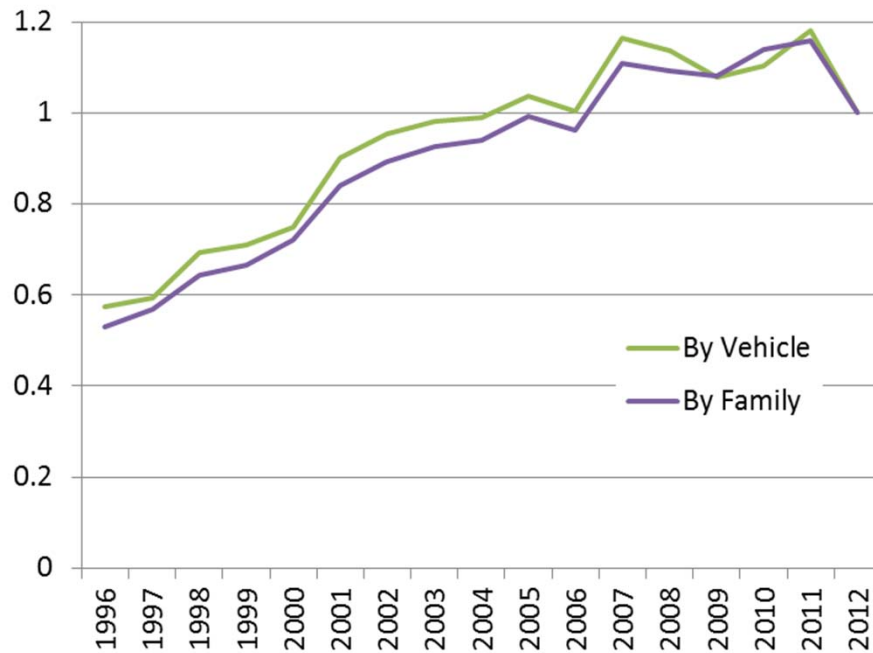
IDA | But there were some issues

- “Negative learning”
 - Most systems show lot-by-lot unit price growth
 - Naïve regression estimates 15% overall annual average
 - Suggests unobserved quality improvements
 - In the aircraft work, year-over-year weight growth was highly significant – proxy for quality improvements
- Price index estimation sensitivity
 - The estimated annual fixed effects are not robust with regard to either subsample or model selection
 - Many models with similar fit, very different annual fixed effects
 - It is possible to get a very good fit without any annual fixed effect terms – what does this indicate?

IDA | Alternative Formulation: The “Pure Price” Model

- Assume that each vehicle model is characterized by
 - An initial unit price
 - An initial quality level
 - A production rate price dependency
 - An unobserved implicit quality growth rate
 - Version 1 – constant by vehicle *family*
 - Version 2 – constant by vehicle *type*
- Estimate unit price as a function of these parameters plus annual fixed effects

IDA | Results in More Stable and Credible Estimates



~ 5.1% average annual price growth

Year	Index (by vehicle)	Index (by family)
1996	48.6%	45.7%
1997	50.3%	49.1%
1998	58.9%	55.5%
1999	60.2%	57.4%
2000	63.4%	62.2%
2001	76.4%	72.6%
2002	80.8%	77.0%
2003	83.2%	80.0%
2004	84.0%	81.2%
2005	88.0%	85.6%
2006	85.0%	83.1%
2007	98.7%	95.8%
2008	96.3%	94.4%
2009	91.3%	93.3%
2010	93.5%	98.3%
2011	100.0%	100.0%

IDA | Summary

- Military vehicle characteristics change too quickly for ordinary price index calculations to apply
- Hedonic models make assumptions that probably aren't true for military vehicles
 - That we know the relevant quality attributes, and have good lot-by-lot data for them
 - That the value to the buyer of a given quality attribute is constant over time
- The pure price model gives stable and credible estimates, but requires one iffy assumption
 - That unobservable quality growth is roughly constant by vehicle type/family

Backup

IDA | Problem Background

- The Weapon Systems Acquisition Reform Act of 2009 (WSARA) tasks OSD(CAPE) with “...assessing and updating the cost indexes that the Department of Defense employs to ensure the use of realistic cost estimates.”
- OSD(CAPE) asked IDA/CARD to assist in assessing the accuracy of existing price indices for various types of system

IDA | What are price indices used for?

- Program offices use price indices to estimate the future budgetary requirements of acquisition programs in then-year dollars
- Oversight organizations use price indices to distinguish sector-specific real price growth from general inflation
- OMB uses price indices to estimate the relative burden of defense procurement (or subsets thereof) on the economy
- **DoD leadership would like to be able to distinguish changes in the price of military capability from changes in the amount of capability demanded**

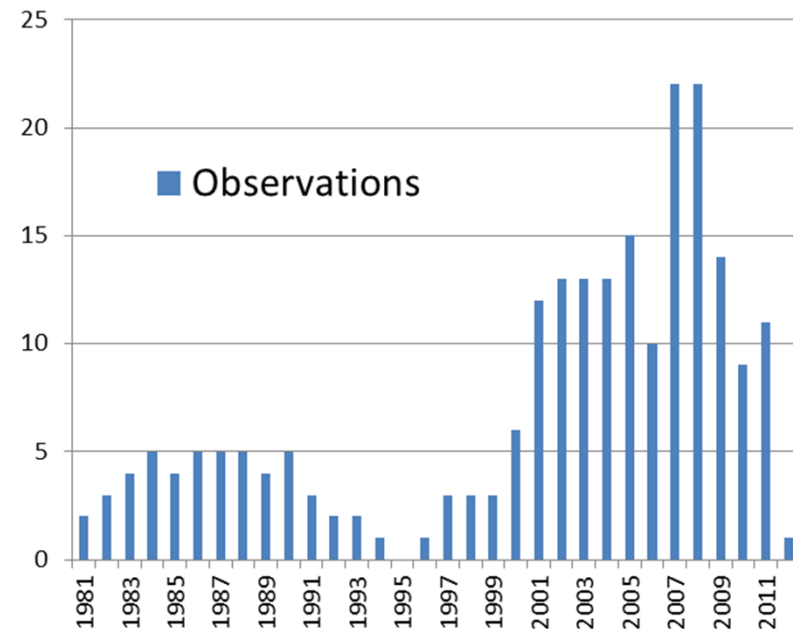
IDA | Data Set

- M1 Abrams tank (2 blocks)
- M2 Bradley Fighting Vehicle (3 blocks)
- M9 Armored Combat Earthmover
- M998 HMMWV (2 blocks)
- M992 Field Artillery Ammunition and Support Vehicle (FAASV) (2 blocks)
- M4 Command and Control Vehicle (C2V)
- Stryker family (8 variants)
- M992A2 FAASV
- Armored Security Vehicle (ASV)
- Family of Heavy Tactical Vehicles (10 variants, ~2 blocks each)
- HMMWV (3 variants)
- MRAP variants
 - Buffalo
 - Cougar H
 - Cougar HE
 - MaxxPro
 - MaxxPro Dash
 - MaxxPro Dash DXM
 - MATV
 - MATV-UIK

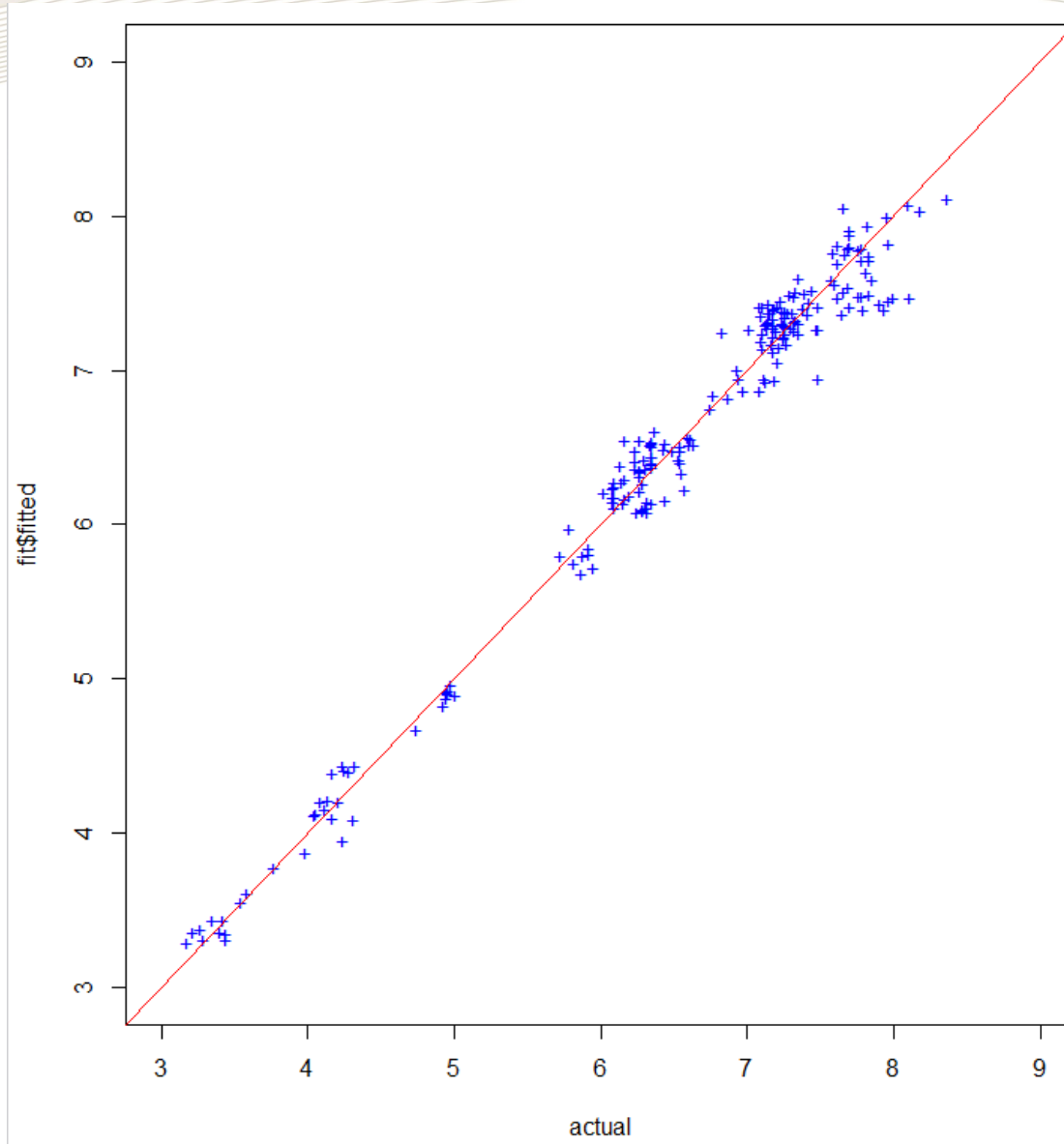
IDA | Yearly Index Significance / Stability

lnd1981	-1.19741	0.23820	-5.027	1.51e-06	***
lnd1982	-0.81351	0.22728	-3.579	0.000475	***
lnd1983	-1.33841	0.19836	-6.747	3.74e-10	***
lnd1984	-1.20171	0.20249	-5.935	2.23e-08	***
lnd1985	-1.30769	0.21043	-6.214	5.63e-09	***
lnd1986	-1.03952	0.19577	-5.310	4.24e-07	***
lnd1987	-1.11364	0.19268	-5.780	4.71e-08	***
lnd1988	-1.17351	0.18638	-6.296	3.74e-09	***
lnd1989	-1.23323	0.19112	-6.453	1.70e-09	***
lnd1990	-1.20646	0.18335	-6.580	8.87e-10	***
lnd1991	-1.21753	0.19325	-6.300	3.67e-09	***
lnd1992	-1.04304	0.25113	-4.153	5.69e-05	***
lnd1993	-1.01753	0.25062	-4.060	8.16e-05	***
lnd1994	-0.85338	0.24998	-3.414	0.000840	***
lnd1996	-0.74025	0.25731	-2.877	0.004650	**
lnd1997	-0.43995	0.21812	-2.017	0.045615	*
lnd1998	-0.61970	0.19555	-3.169	0.001882	**
lnd1999	-0.37114	0.17559	-2.114	0.036326	*
lnd2000	-0.11998	0.15745	-0.762	0.447349	
lnd2001	-0.10971	0.13765	-0.797	0.426786	
lnd2002	-0.07241	0.13645	-0.531	0.596487	
lnd2003	-0.11813	0.13609	-0.868	0.386871	
lnd2004	-0.01696	0.13884	-0.122	0.902974	
lnd2005	-0.04658	0.13319	-0.350	0.727042	
lnd2006	-0.10858	0.13772	-0.788	0.431821	
lnd2007	0.02043	0.12931	0.158	0.874663	
lnd2008	0.03024	0.12840	0.236	0.814165	
lnd2009	0.01292	0.13822	0.093	0.925669	
lnd2010	0.05820	0.14082	0.413	0.680008	

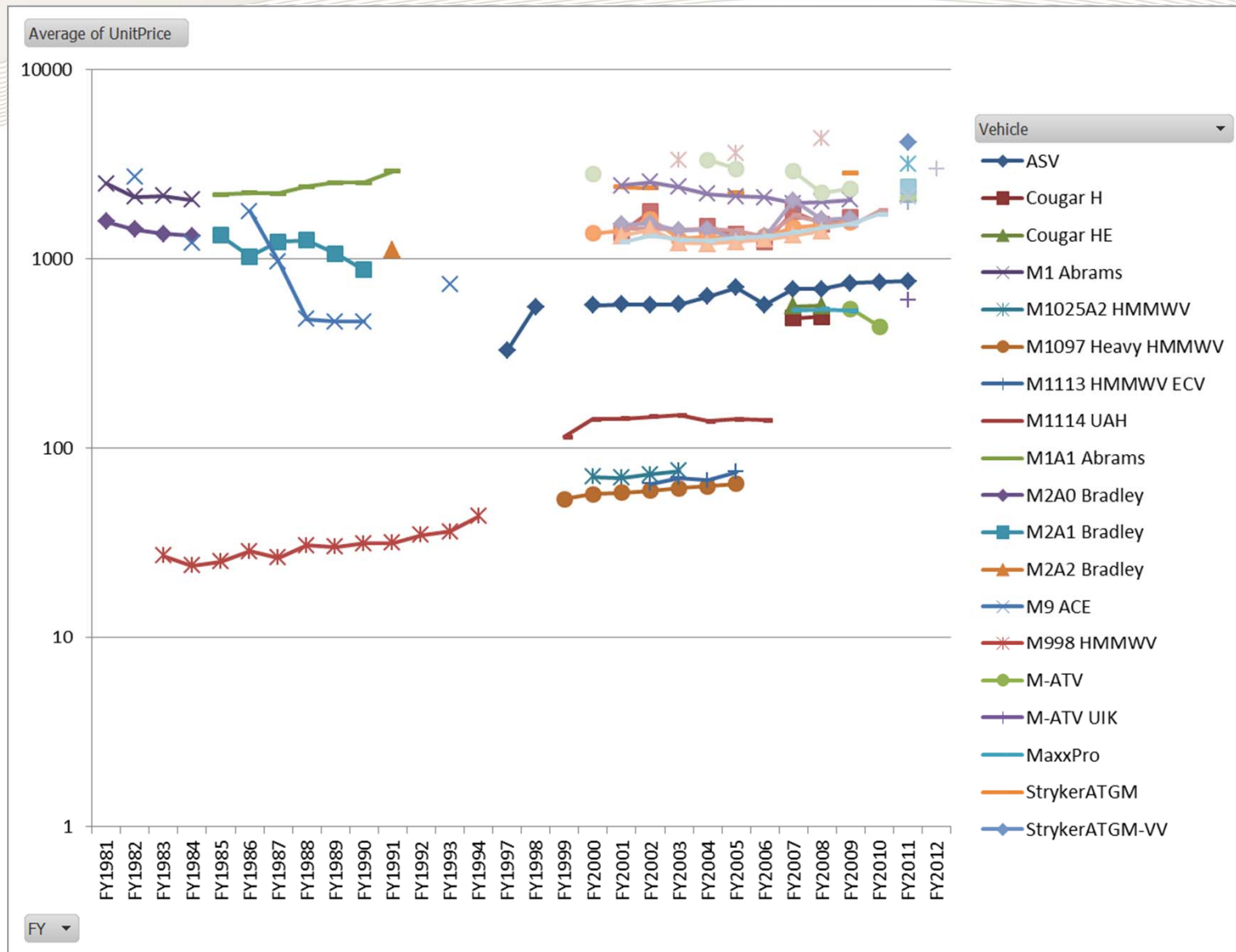
Vehicle buys by year



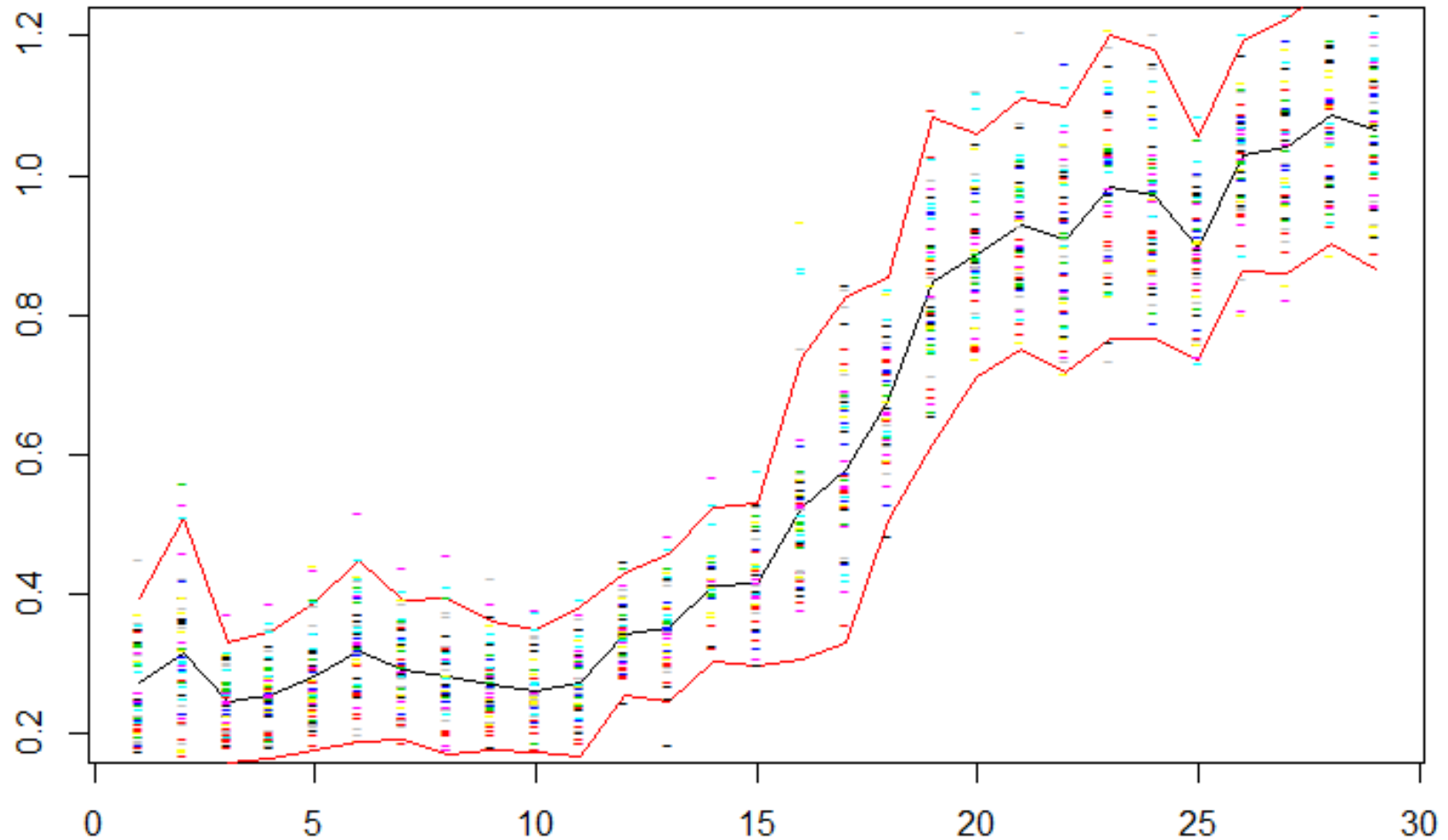
IDA | Predicted vs. Actual Log (Lot Price)



IDA | Negative Learning



IDA | High Standard Error for Annual Fixed Effects



IDA | Model Specification

$$\ln(U_j) = \beta_0 + \sum_{k=1}^V \beta_k I_{jk} + \sum_{k=1}^V \beta_{V+k} I_{jk} \ln(N_j) + \beta_{2V+1} \ln(Q_j) + \sum_{t=1}^T \alpha_t Y_{jt}$$

U_j = unit price of purchase j

V = number of vehicle types

Q_j = lot size of purchase j

N_j = lot number of purchase j

$I_{jk} = \mathbf{1}\{ \text{purchase } j \text{ is of vehicle type } k \}$

T = number of years covered by purchases

$Y_{jt} = \mathbf{1}\{ \text{purchase } j \text{ was in year } t \}$

$\text{Exp}(\alpha_t)$ = price index for year t

IDA | Way Forward

- Compile more data
 - Medium tactical vehicles
 - Fill the 1994–95 gap; extend beyond 2011
- Bootstrap to reduce the variance of the pure price model estimates as well
- Explore models with no lot size effect
 - Should an ideal price index describe price growth for fixed quality and quantity, or just quality?

REPORT DOCUMENTATION PAGE

*Form Approved
OMB No. 0704-0188*

The public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing the burden, to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number.

PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.

1. REPORT DATE (DD-MM-YYYY)		2. REPORT TYPE		3. DATES COVERED (From - To)	
4. TITLE AND SUBTITLE				5a. CONTRACT NUMBER	
				5b. GRANT NUMBER	
				5c. PROGRAM ELEMENT NUMBER	
6. AUTHOR(S)				5d. PROJECT NUMBER	
				5e. TASK NUMBER	
				5f. WORK UNIT NUMBER	
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)				8. PERFORMING ORGANIZATION REPORT NUMBER	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)				10. SPONSOR/MONITOR'S ACRONYM(S)	
				11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT					
13. SUPPLEMENTARY NOTES					
14. ABSTRACT					
15. SUBJECT TERMS					
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
a. REPORT	b. ABSTRACT	c. THIS PAGE			19b. TELEPHONE NUMBER (Include area code)

